We analyze several classes of nonlinear eigenvalue problems associated to non-homogeneous differential operators. We point out some striking results with respect to the classical theory of linear differential operators. The proofs rely mainly on variational methods (Ekeland’s variational principle, semi-continuity arguments). Some open problems are also raised during the lectures.